

# Slepton Production in $e^-e^-$ -Collisions

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- Motivation

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- Process

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- Neutralino Sector

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- LR-Mixing

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- Threshold Behaviour

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- Summary

$$e^- e^- \longrightarrow \tilde{l}_i \tilde{l}_j$$

- high cross sections

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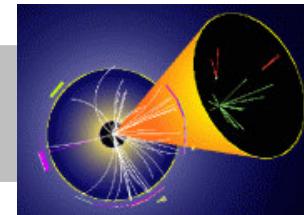
- high cross sections
- distinctive threshold

$$e^- e^- \longrightarrow \tilde{l}_i \tilde{l}_j$$

- high cross sections
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- high beam polarisation

$$e^- e^- \longrightarrow \tilde{l}_i \tilde{l}_j$$

- high cross sections
- distinctive threshold
- high beam polarisation
- special polarisation dependence

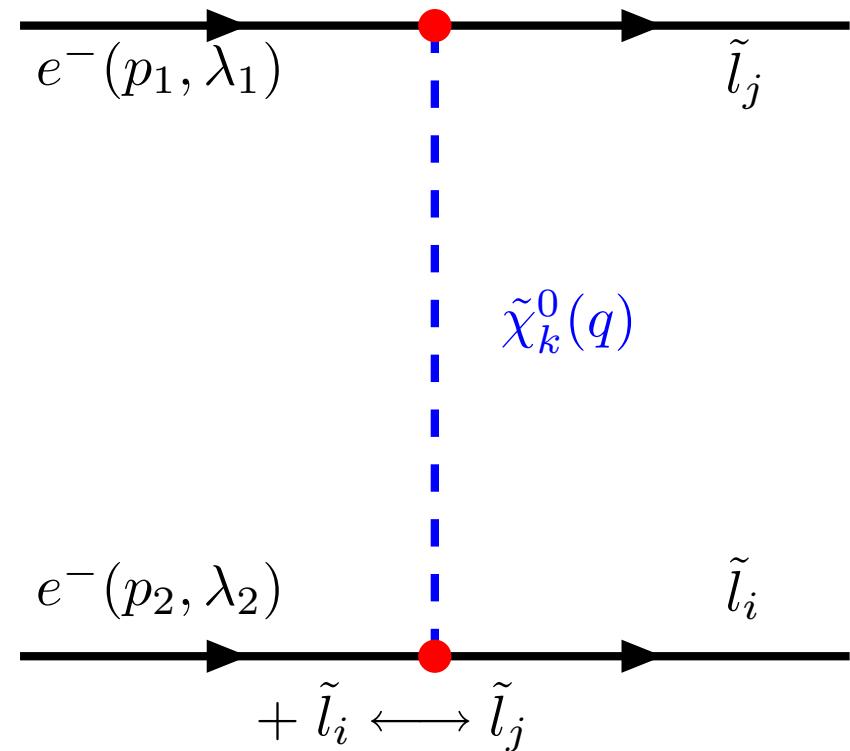


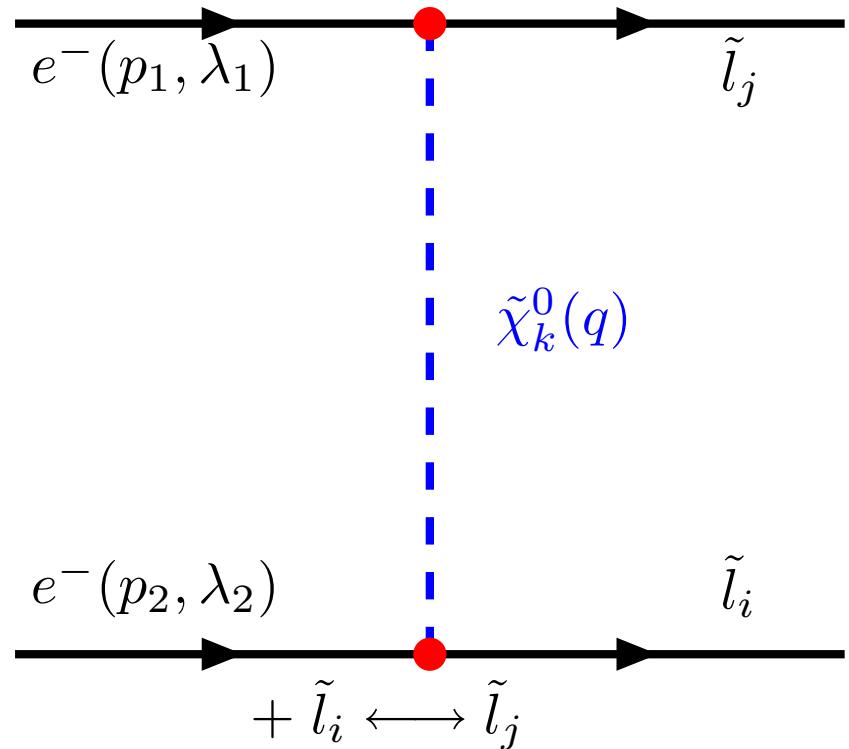
$$e^- e^- \longrightarrow \tilde{l}_i \tilde{l}_j$$

- high cross sections
- distinctive threshold
- high beam polarisation
- special polarisation dependence
- low background

}

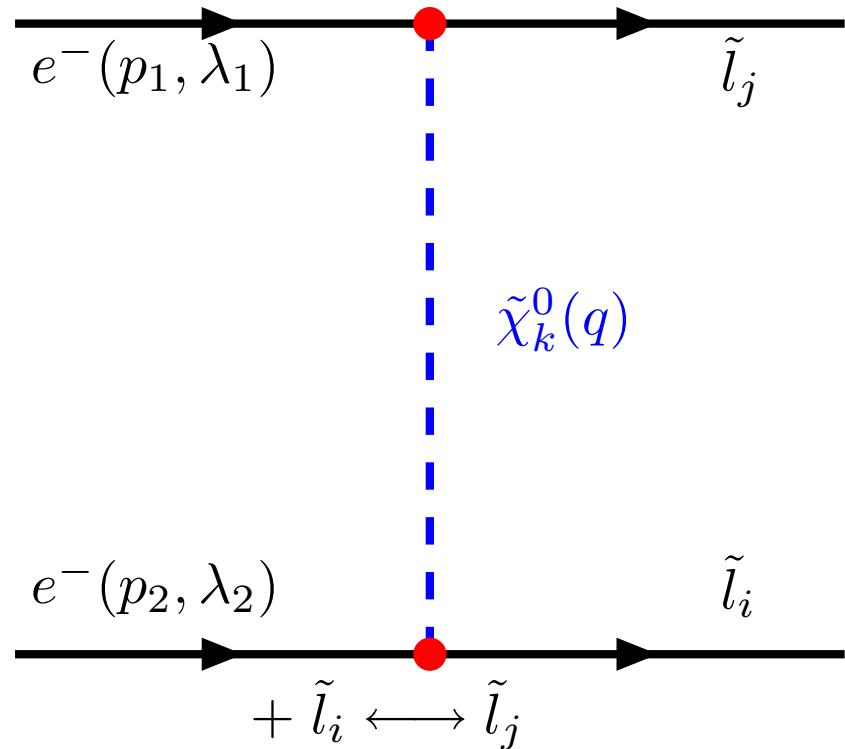
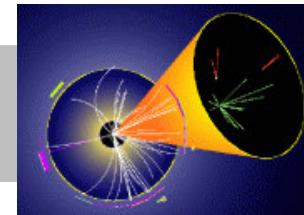
high sensitivity to  $\tilde{l}$ - and  
 $\tilde{\chi}^0$ -properties





Amplitude (t-Channel)

$$\begin{aligned} T_{i,j}^{\lambda_1 \lambda_2}(\tilde{\chi}_k^0) &= g^2 \bar{v}(p_2, \lambda_2) \\ &\quad (a_k^{mi^*} P_L + b_k^{mi^*} P_R) \\ &\quad \Delta_t^k(\not{q} + m_{\tilde{\chi}_k^0}) \\ &\quad (a_k^{mj^*} P_L + b_k^{mj^*} P_R) \\ &\quad u(p_1, \lambda_1) \end{aligned}$$



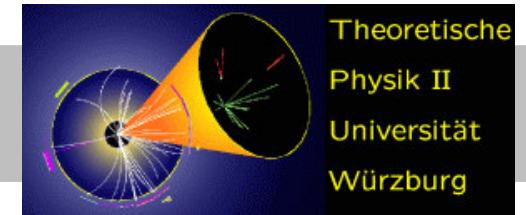
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- neutralino exchange  $\Rightarrow$  massive fermion propagator
- Including LR and Flavour Mixing

(Hikasa, 1986; Blöchinger et.al., 2002; Arkani-Hamed et al. hep-ph/9704205)

# Neutralino Mass Matrix



$$Y = \begin{pmatrix} M_2 s_W^2 + M_1 c_W^2 & (M_2 - M_1) s_W c_W & 0 & 0 \\ (M_2 - M_1) s_W c_W & M_2 c_W^2 s_W^2 & m_Z & 0 \\ 0 & m_Z & \mu s_{2\beta} & -\mu c_{2\beta} \\ 0 & 0 & -\mu c_{2\beta} & -\mu s_{2\beta} \end{pmatrix}$$

Basis:  $\tilde{\gamma}, \tilde{Z}, \tilde{H}_a^0, \tilde{H}_b^0$ ; GUT:  $M_1 = \frac{5}{3} \tan^2 \theta_W M_2$

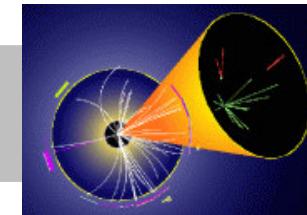
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Diagonalisation with matrix  $N$ :  $N^* Y N^{-1} = M_D$   
 gives Down-Lepton-Slepton-Neutralino-Couplings

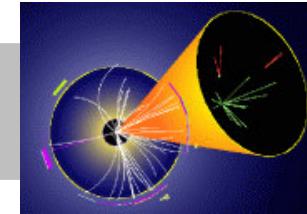
$$\begin{aligned} f_k^L &= \sqrt{2} \left[ \frac{1}{\cos \theta_W} \left( \frac{1}{2} - \sin^2 \theta_W \right) N_{k2} + \sin \theta_W \right] \\ f_k^R &= \sqrt{2} \sin \theta_W (\tan \theta_W N_{k2} - N_{k1}) \end{aligned}$$



Slepton mass matrix (in MSSM):

$$\mathcal{M}_{\tilde{l}}^2 = \begin{pmatrix} M_L^2 + m_l^2 + D_L & m_l(A_l - \mu \tan \beta) \\ m_l(A_l - \mu \tan \beta) & M_E^2 + m_l^2 + D_R \end{pmatrix} = \begin{pmatrix} m_{LL}^2 & m_{LR}^2 \\ m_{LR}^2 & m_{RR}^2 \end{pmatrix}$$

where  $D_L = (-\frac{1}{2} + \sin^2 \theta_W) \cos(2\beta) m_Z^2$  and  $D_R = -\sin^2 \theta_W \cos(2\beta) m_Z^2$



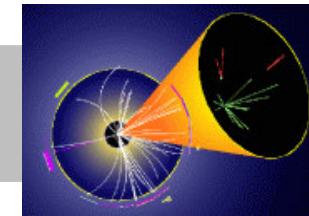
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Slepton LR-Mixing:

$$\begin{pmatrix} \tilde{l}_1 \\ \tilde{l}_2 \end{pmatrix} = \begin{pmatrix} \cos \theta_{\tilde{l}} & \sin \theta_{\tilde{l}} \\ -\sin \theta_{\tilde{l}} & \cos \theta_{\tilde{l}} \end{pmatrix} \begin{pmatrix} \tilde{l}_L \\ \tilde{l}_R \end{pmatrix}$$



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The couplings are given by

$$a_k^{e2} = f_k^L \cos \theta_{\tilde{l}} \quad a_k^{e1} = -f_k^L \sin \theta_{\tilde{l}}$$

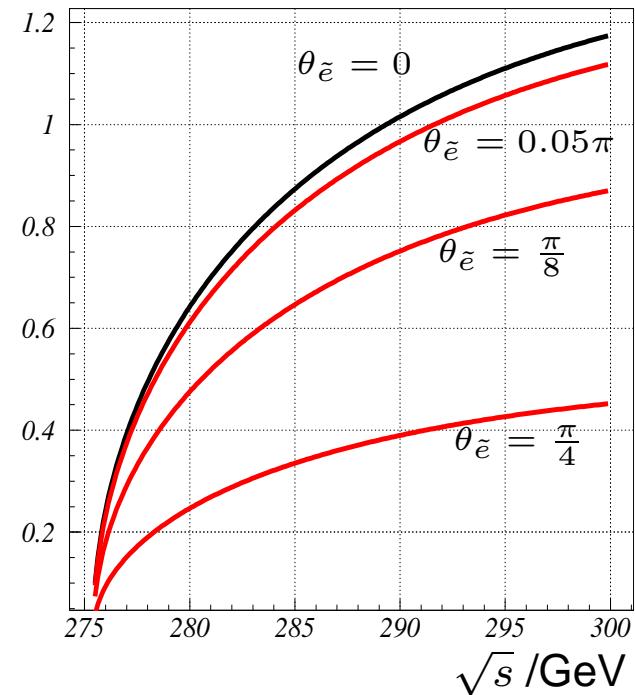
$$b_k^{e2} = f_k^R \sin \theta_{\tilde{l}} \quad b_k^{e1} = f_k^R \cos \theta_{\tilde{l}}$$

Production of  $\tilde{l}_R \tilde{l}_R$

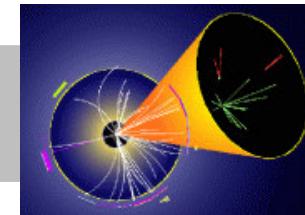
(similar for  $\tilde{l}_L \tilde{l}_L$ )

$\Rightarrow$  Threshold:  $\propto \beta$

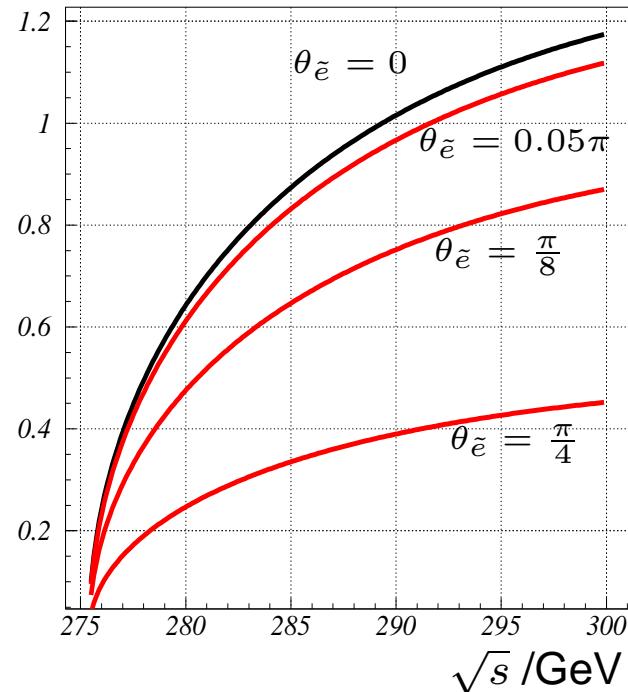
$\sigma / \text{pb}$



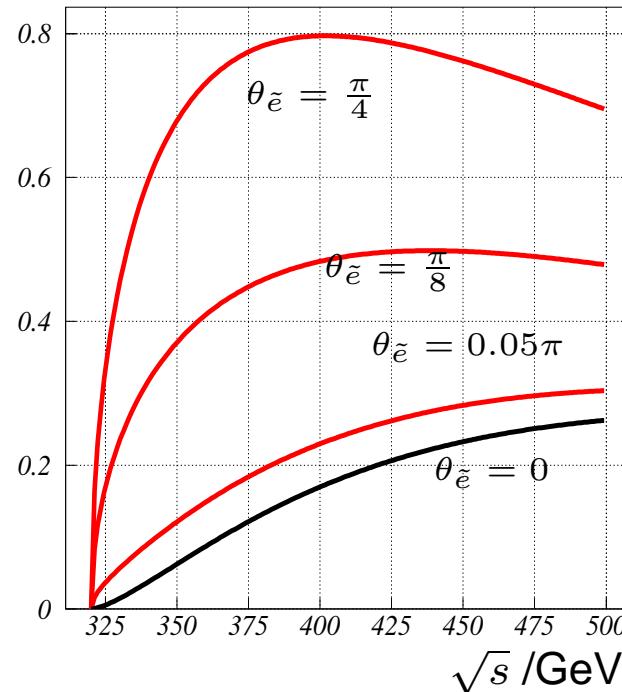
# Threshold Behaviour



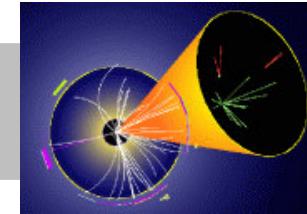
Production of  $\tilde{l}_R \tilde{l}_R$   
(similar for  $\tilde{l}_L \tilde{l}_L$ )  
 $\Rightarrow$  Threshold:  $\propto \beta$

 $\sigma / \text{pb}$ 

Production of  $\tilde{l}_L \tilde{l}_R$   
 $\Rightarrow$  Threshold:  $\propto \beta^3$   
**BUT:**  $\propto \beta$  with LR-Mixing

 $\sigma / \text{pb}$ 

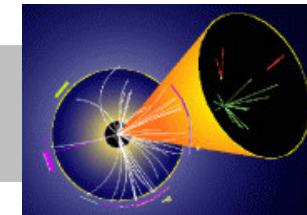
No beam polarisation necessary!



Most general form of Flavour Mixing Matrix:

$$W_i = \begin{pmatrix} c_{\phi_{12}^i} c_{\phi_{13}^i} & s_{\phi_{12}^i} c_{\phi_{13}^i} & s_{\phi_{13}^i} e^{-i\delta} \\ -s_{\phi_{12}^i} c_{\phi_{23}^i} - c_{\phi_{12}^i} s_{\phi_{23}^i} s_{\phi_{13}^i} e^{i\delta} & c_{\phi_{12}^i} c_{\phi_{23}^i} - s_{\phi_{12}^i} s_{\phi_{23}^i} s_{\phi_{13}^i} e^{i\delta} & s_{\phi_{13}^i} c_{\phi_{13}^i} \\ s_{\phi_{12}^i} s_{\phi_{23}^i} - c_{\phi_{12}^i} c_{\phi_{23}^i} s_{\phi_{13}^i} e^{i\delta} & -c_{\phi_{12}^i} s_{\phi_{23}^i} - s_{\phi_{12}^i} c_{\phi_{23}^i} s_{\phi_{13}^i} e^{i\delta} & c_{\phi_{23}^i} c_{\phi_{12}^i} \end{pmatrix}$$

$i$ : L or R,  $\phi_{12}^i, \phi_{23}^i, \phi_{13}^i$ : Mixing angles,  $\delta$ : CP-phase (Arkani-Hamed et al. hep-ph/9704205)



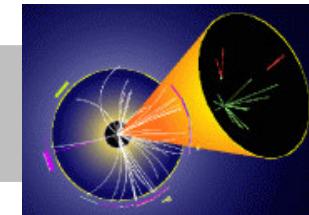
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Full mixing matrix for all three generations left and right:

$$W = \begin{pmatrix} W_L & 0 \\ 0 & W_R \end{pmatrix}$$



Most general form of Flavour Mixing Matrix:

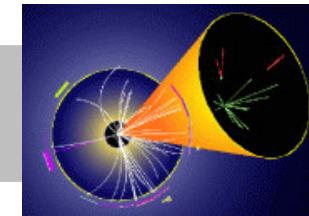
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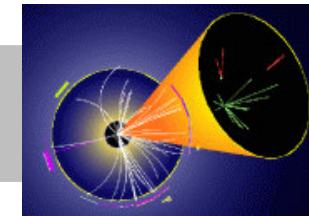
$$W = \begin{pmatrix} W_L & 0 \\ 0 & W_R \end{pmatrix}$$

Note: Does **not** include **LR-Mixing**



To incorporate both Flavour- and LR-Mixing:

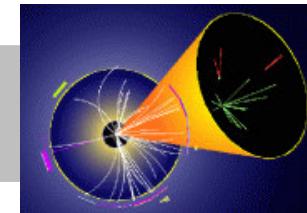
$$\begin{aligned} M^2 &= \textcolor{red}{L} W M_D^2 W^\dagger \textcolor{red}{L}^\dagger \\ &= \begin{pmatrix} 0 & L_L \\ L_R & 0 \end{pmatrix} \begin{pmatrix} W_L & 0 \\ 0 & W_R \end{pmatrix} \begin{pmatrix} M_L & 0 \\ 0 & M_R \end{pmatrix}^2 \begin{pmatrix} W_L^\dagger & 0 \\ 0 & W_R^\dagger \end{pmatrix} \begin{pmatrix} 0 & \textcolor{red}{L}_R^\dagger \\ \textcolor{red}{L}_L^\dagger & 0 \end{pmatrix} \end{aligned}$$



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Affects the couplings:  $\alpha = 1..3$ : Lepton,  $m = 1..3$ : Slepton,  $k = 1..4$ : Neutralino



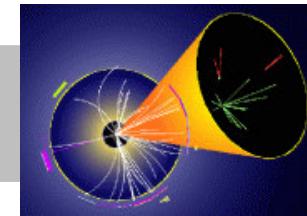
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$$f_{\alpha k}^L \rightarrow f_{\alpha k}^L W^{m\alpha} \quad f_{\alpha k}^R \rightarrow f_{\alpha k}^R W^{(m+3)\alpha}$$



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$$a_k^{m2} = \cos \theta_{\tilde{l}} f_{\alpha k}^L W^{\alpha m}; \quad a_k^{m1} = -\sin \theta_{\tilde{l}} f_{\alpha k}^L W^{\alpha(m+3)}$$

$$b_k^{m2} = \sin \theta_{\tilde{l}} f_{\alpha k}^R W^{\alpha m}; \quad b_k^{m1} = \cos \theta_{\tilde{l}} f_{\alpha k}^R W^{\alpha(m+3)}$$

## ● Density Matrix Formalism (Bouchiat-Michel-Formulae)

(Nucl. Phys. B 5 (1958) p. 416)

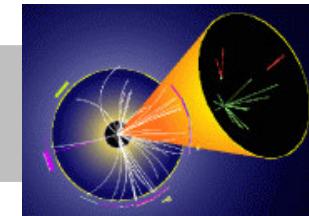
$$\begin{aligned} u(p, \lambda') \bar{u}(p, \lambda) = & \frac{1}{2} (1 + 2\lambda\gamma_5) \delta_{\lambda\lambda'} \cdot \not{p} \\ & + \frac{1}{2} \gamma_5 (\not{s}^1 \sigma_{\lambda\lambda'}^1 + \not{s}^2 \sigma_{\lambda\lambda'}^2) \cdot \not{p} \end{aligned}$$

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## ● massive fermion propagator: $\propto (\not{q} + m_{\tilde{\chi}^0})$



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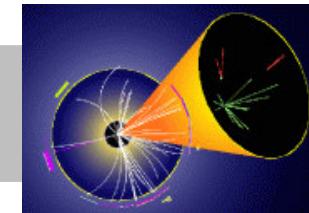
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- massive fermion propagator:  $\propto (\not{q} + m_{\tilde{\chi}^0})$

⇒ Contributions in transverse polarisation?

Squared amplitude:

$$\propto \text{Tr} \left\{ [u(p_1, \lambda'_1) \bar{u}(p_1, \lambda_1)] (\not{q} + m_{\tilde{\chi}_k^0}) [v(p_2, \lambda'_2) \bar{v}(p_2, \lambda_2)] (\not{q} + m_{\tilde{\chi}_l^0}) \right\}$$



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Bouchiat-Michel-Formulae yield e.g.:

$$\underbrace{\cdots \delta_{\lambda_1, \lambda'_1} \not{p}_1 \cdots}_{\text{long. and unpol. contrib.}} (\not{q} + m_{\tilde{\chi}_k^0}) \underbrace{\cdots \not{s}^a \sigma_{\lambda_2, \lambda'_2}^a \not{p}_2 \cdots}_{\text{transverse contrib.}} (\not{q} + m_{\tilde{\chi}_k^0})$$

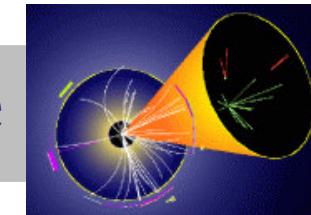
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$$\propto \text{Tr} \left\{ [u(p_1, \lambda'_1) \bar{u}(p_1, \lambda_1)] (\not{q} + m_{\tilde{\chi}_k^0}) [v(p_2, \lambda'_2) \bar{v}(p_2, \lambda_2)] (\not{q} + m_{\tilde{\chi}_l^0}) \right\}$$

Bouchiat-Michel-Formulae yield e.g.:

$$\underbrace{\cdots \delta_{\lambda_1, \lambda'_1} \not{p}_1 \cdots}_{\text{long. and unpol. contrib.}} (\not{q} + m_{\tilde{\chi}_k^0}) \underbrace{\cdots \not{s}^a \sigma_{\lambda_2, \lambda'_2}^a \not{p}_2 \cdots}_{\text{transverse contrib.}} (\not{q} + m_{\tilde{\chi}_k^0})$$

⇒ Contributions linear in the transverse polarisation



Squared amplitude:

$$\propto \text{Tr} \left\{ [u(p_1, \lambda'_1) \bar{u}(p_1, \lambda_1)] (\not{q} + m_{\tilde{\chi}_k^0}) [v(p_2, \lambda'_2) \bar{v}(p_2, \lambda_2)] (\not{q} + m_{\tilde{\chi}_l^0}) \right\}$$

Bouchiat-Michel-Formulae yield e.g.:

$$\underbrace{\cdots \delta_{\lambda_1, \lambda'_1} \not{p}_1 \cdots}_{\text{long. and unpol. contrib.}} (\not{q} + m_{\tilde{\chi}_k^0}) \underbrace{\cdots \not{s}^a \sigma_{\lambda_2, \lambda'_2}^a \not{p}_2 \cdots}_{\text{transverse contrib.}} (\not{q} + m_{\tilde{\chi}_k^0})$$

⇒ Contributions linear in the transverse polarisation

Contributions of all polarisation combinations,  
transverse as well as longitudinal.

$$\bullet \propto (1 \pm P_1^L)(1 \pm P_2^L) \cdot a_k^{mi*} b_k^{mj*} a_l^{mi} b_l^{mj} \cdot [(p_1, p_2, q) \dots]$$

( $k, l = 1..4$ : Neutralinos;  $i, j = 1, 2$  ("L,R"): Slepton,  $m = 1..3$ : Slepton flavour)

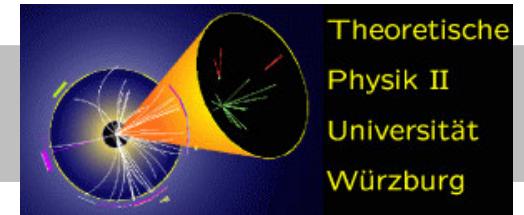
- $\propto (1 \pm P_1^L)(1 \pm P_2^L) \cdot a_k^{mi*} b_k^{mj*} a_l^{mi} b_l^{mj} \cdot [(p_1, p_2, q) \dots]$
- $\propto \pm P_{1,2}^T (1 \pm P_{2,1}^L) \cdot a_k^{mi*} b_k^{mj*} a_l^{mj} a_l^{mi} \cdot [(\cdot, \cdot) + \varepsilon_{\mu\nu\rho\sigma} \dots]$

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# Overall Structure



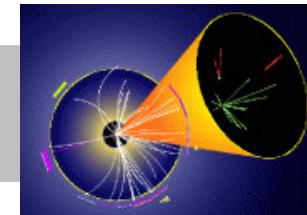
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# Overall Structure

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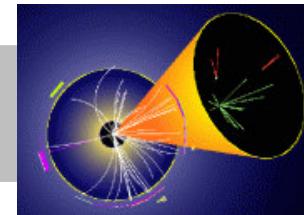
- $\propto (1 \pm P_1^L)(1 \pm P_2^L) \cdot a_k^{mi*} b_k^{mj*} a_l^{mi} b_l^{mj} \cdot [(p_1, p_2, q) \dots]$
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( $k, l = 1..4$ : Neutralinos;  $i, j = 1, 2$  ("L,R"): Slepton,  $m = 1..3$ : Slepton flavour)

With the couplings:

$$\begin{aligned} a_k^{m2} &= \cos \theta_{\tilde{l}} f_{\alpha k}^L W^{\alpha m}; & a_k^{m1} &= -\sin \theta_{\tilde{l}} f_{\alpha k}^L W^{\alpha(m+3)} \\ b_k^{m2} &= \sin \theta_{\tilde{l}} f_{\alpha k}^R W^{\alpha m}; & b_k^{m1} &= \cos \theta_{\tilde{l}} f_{\alpha k}^R W^{\alpha(m+3)} \end{aligned}$$

# Overall Structure



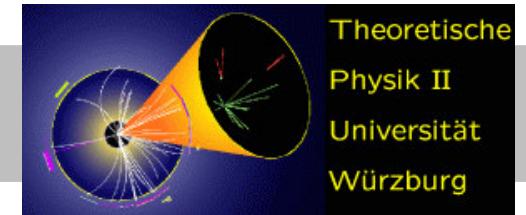
	$\tilde{l}_i \tilde{l}_i$	$ T ^2$	$TU^*$	$\tilde{l}_i \tilde{l}_j$	$ T ^2$	$TU^*$
$(1 + P_1^L)(1 - P_2^L)$	$c^2 s^2$		$c^2 s^2$		$c^4$	$-c^2 s^2$
$(1 - P_1^L)(1 + P_2^L)$	$c^2 s^2$		$c^2 s^2$		$s^4$	$-c^2 s^2$
$(1 - P_1^L)(1 - P_2^L)$	$c^4$		$c^4$		$c^2 s^2$	$c^2 s^2$
$(1 + P_1^L)(1 + P_2^L)$	$s^4$		$s^4$		$s^2 c^2$	$s^2 c^2$
$P_{1,2}^T (1 - P_{2,1}^L) m_{\tilde{\chi}_l^0}$	$c^3 s$	CP	$c^3 s$	CP	$-c^2 s^2$	CP
$P_{1,2}^T (1 + P_{2,1}^L) m_{\tilde{\chi}_l^0}$	$s^3 c$	CP	$s^3 c$	CP	$-c^2 s^2$	CP
$P_{1,2}^T (1 - P_{2,1}^L) m_{\tilde{\chi}_k^0}$	$c^3 s$	CP	$c^3 s$	CP	$-c^3 s$	CP
$P_{1,2}^T (1 + P_{2,1}^L) m_{\tilde{\chi}_k^0}$	$-s^3 c$	CP	$-s^3 c$	CP	$-s^2 c^2$	CP
$P_1^T P_2^T$	$\pm c^2 s^2$	CP	$\pm c^2 s^2$	CP	$c^4 \pm s^4$	CP
					$c^2 s^2$	CP

$$c = \cos \theta_{\tilde{l}} \text{ and } s = \sin \theta_{\tilde{l}}$$

$|U|^2$  and  $UT^*$  analogous; “CP” marks CP sensitive contributions

$\langle \uparrow \diamond \downarrow \rangle$

# Flavour Mixing



- $e^- e^- \longrightarrow \tilde{\tau}_i \tilde{\tau}_j$     **2 flavour mixing vertices**  $\Rightarrow$  low cross section

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However: **Asymmetric Channels** only **1 flavour mixing** vertex

- $e^- e^- \rightarrow \tilde{\tau}_i \tilde{\tau}_j$     **2 flavour mixing** vertices  $\Rightarrow$  low cross section
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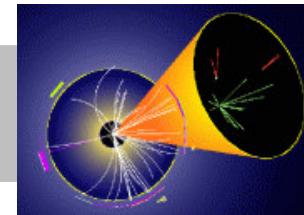
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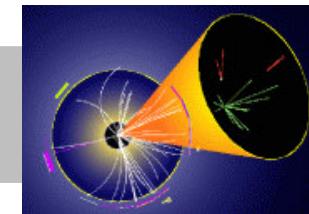
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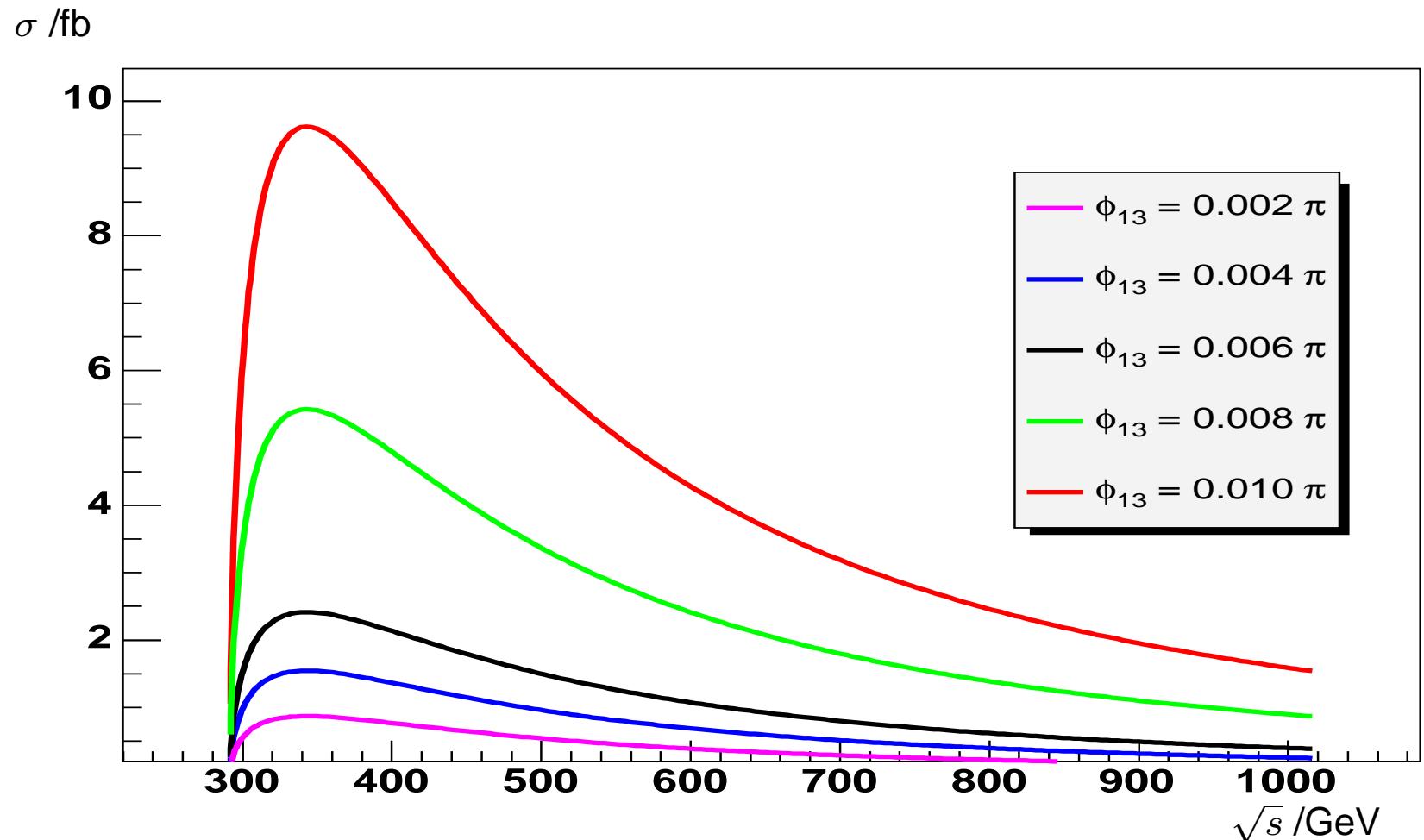
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$$\left. \begin{array}{l} \bullet \quad e^- e^- \rightarrow \tilde{\tau}_i \tilde{e}_j \\ \bullet \quad e^- e^- \rightarrow \tilde{\mu}_i \tilde{e}_j \end{array} \right\} \quad \begin{array}{l} \text{Access to Contributions} \\ \propto P^T(1 \pm P^L) \\ \textcircled{?} \quad \textbf{LR-Mixing: } \theta_{\tilde{\tau}} \\ \textcircled{?} \quad \textbf{Flavour Mixing: } \phi_{12}, \phi_{13} \\ \textcircled{?} \quad \textbf{Asymmetries} \end{array}$$



$e^- e^- \longrightarrow \tilde{\tau}_1 \tilde{e}_R$ : SPS1a-like Scenario,  $P_1^T = P_2^L = 80\%$   
 $\phi_{12} = 0, \phi_{23} = 0$



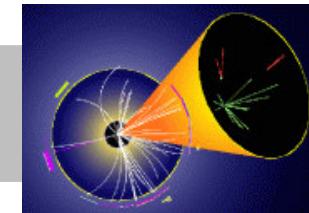
From the Flavour Mixing Matrix  $W$  assuming  $\phi_{12} = \phi_{23} = 0$

$$W^i = \begin{pmatrix} \cos \phi_{13}^i & 0 & \sin \phi_{13}^i e^{i\delta} \\ 0 & 1 & 0 \\ -\sin \phi_{13}^i e^{i\delta} & 0 & 1 \end{pmatrix}$$

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$\Rightarrow$  Expect only low sensitivity of asymmetries to  $\phi_{13}^i$  for small values  
as  $\sigma \propto \sin^2 \phi_{13}^i$

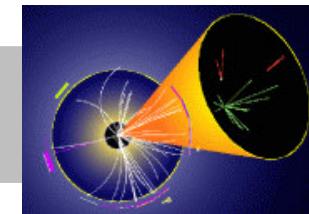


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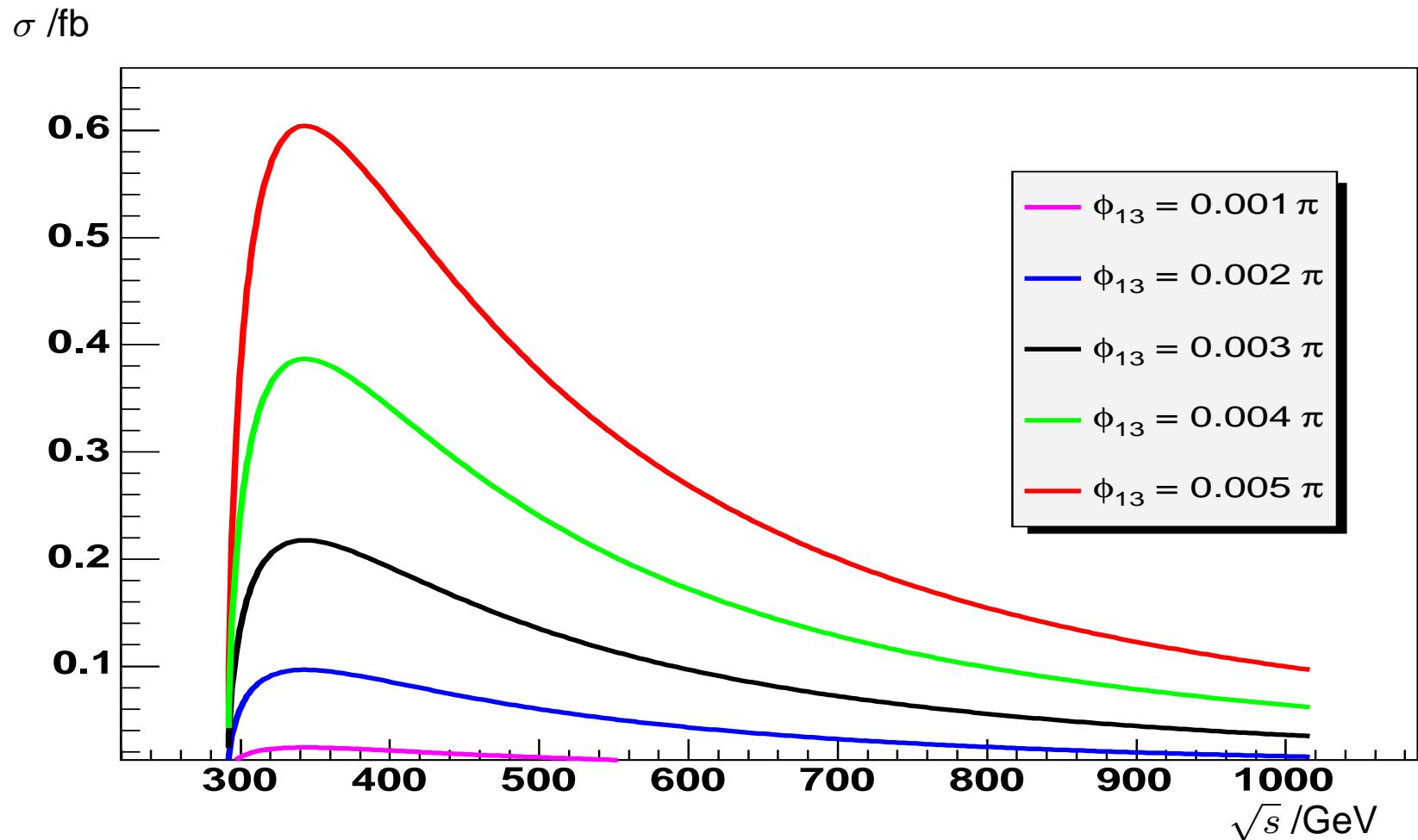
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as  $\sigma \propto \sin^2 \phi_{13}^i$

But: strong dependence of  $\sigma$  on  $\phi_{13}$



$e^- e^- \longrightarrow \tilde{\tau}_1 \tilde{e}_R$ : SPS1a-like Scenario,  $P_1^T = P_2^L = 80\%$   
 $\phi_{12} = 0 = \phi_{23} = 0$



Polarisation asymmetry:

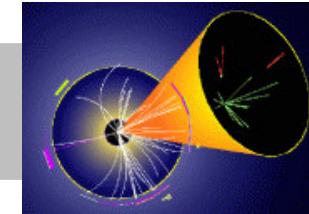
$$A_\sigma = \frac{\sigma(P_1^A, P_1^B) - \sigma(P_2^A, P_2^B)}{\sigma(P_1^A, P_1^B) + \sigma(P_2^A, P_2^B)}$$

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Differential polarisation asymmetry:

$$A_{d\sigma} = \frac{\frac{d}{d\theta}\sigma(P_1^A, P_1^B) - \frac{d}{d\theta}\sigma(P_2^A, P_2^B)}{\frac{d}{d\theta}\sigma(P_1^A, P_1^B) + \frac{d}{d\theta}\sigma(P_2^A, P_2^B)}$$



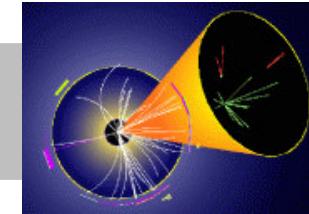
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If one configuration is  $P^L P^T$ :



Polarisation asymmetry:

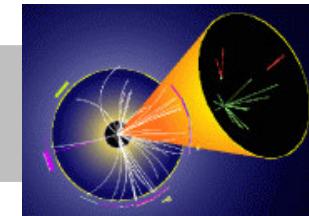
$$A_\sigma = \frac{\sigma(P_1^A, P_1^B) - \sigma(P_2^A, P_2^B)}{\sigma(P_1^A, P_1^B) + \sigma(P_2^A, P_2^B)}$$

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If one configuration is  $P^L P^T$ :

- Selects the terms linear in  $P^T$



Polarisation asymmetry:

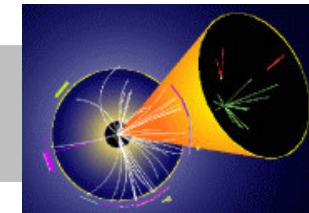
$$A_\sigma = \frac{\sigma(P_1^A, P_1^B) - \sigma(P_2^A, P_2^B)}{\sigma(P_1^A, P_1^B) + \sigma(P_2^A, P_2^B)}$$

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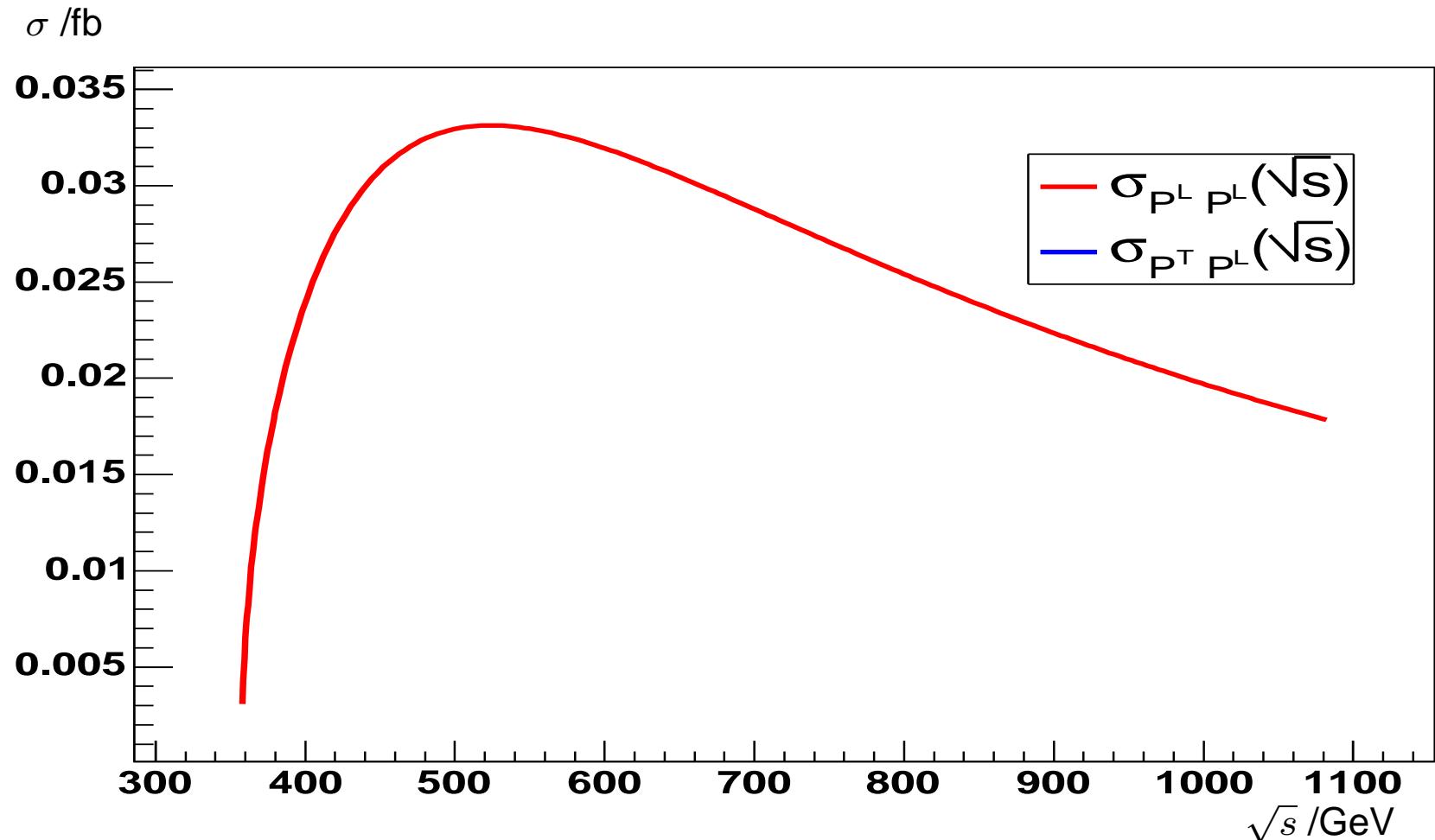
If one configuration is  $P^L P^T$ :

- Selects the terms linear in  $P^T$
- Sensitive to **LR-Mixing**

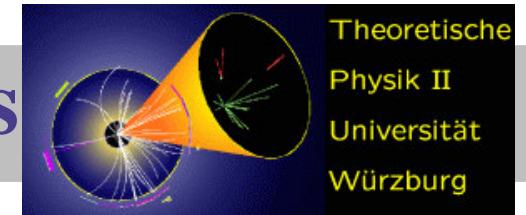
$\langle \uparrow \diamond \downarrow \rangle$  $e^- e^- \longrightarrow \tilde{\tau}_1 \tilde{e}_L$ 

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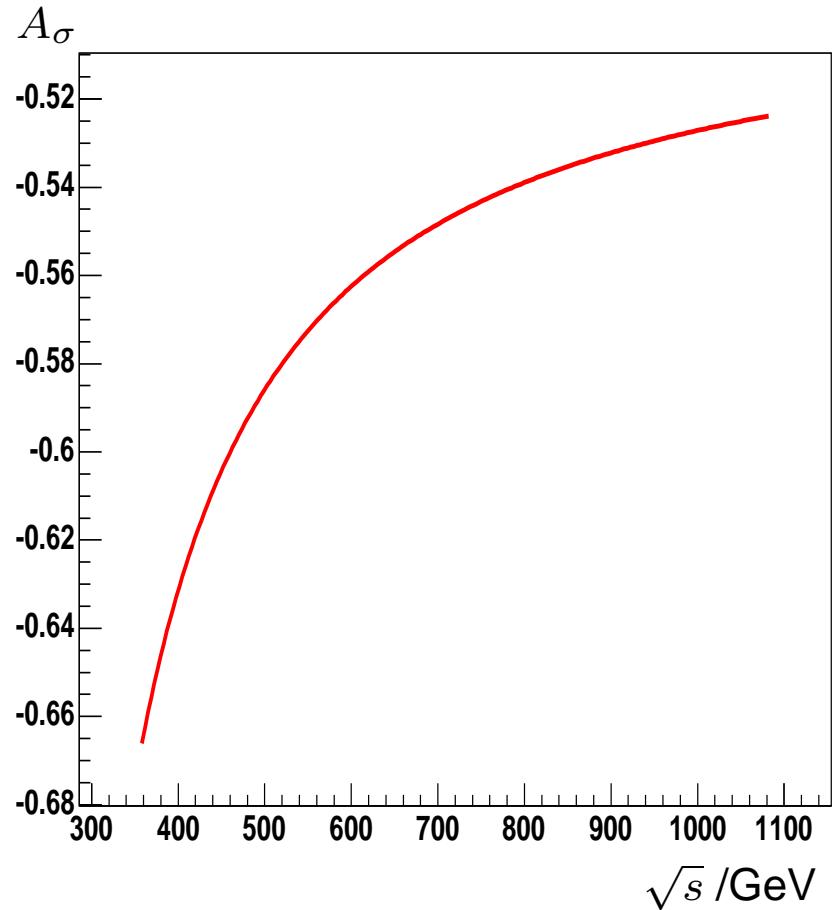
**SPS1a-like Scenario,**  $P_1^T = P_2^L = 80\%$   
 $\phi_{12} = \phi_{23} = 0, \phi_{13} = 0.008, \theta_{\tilde{\tau}} = \frac{\pi}{4}$



# Polarisation Asymmetries

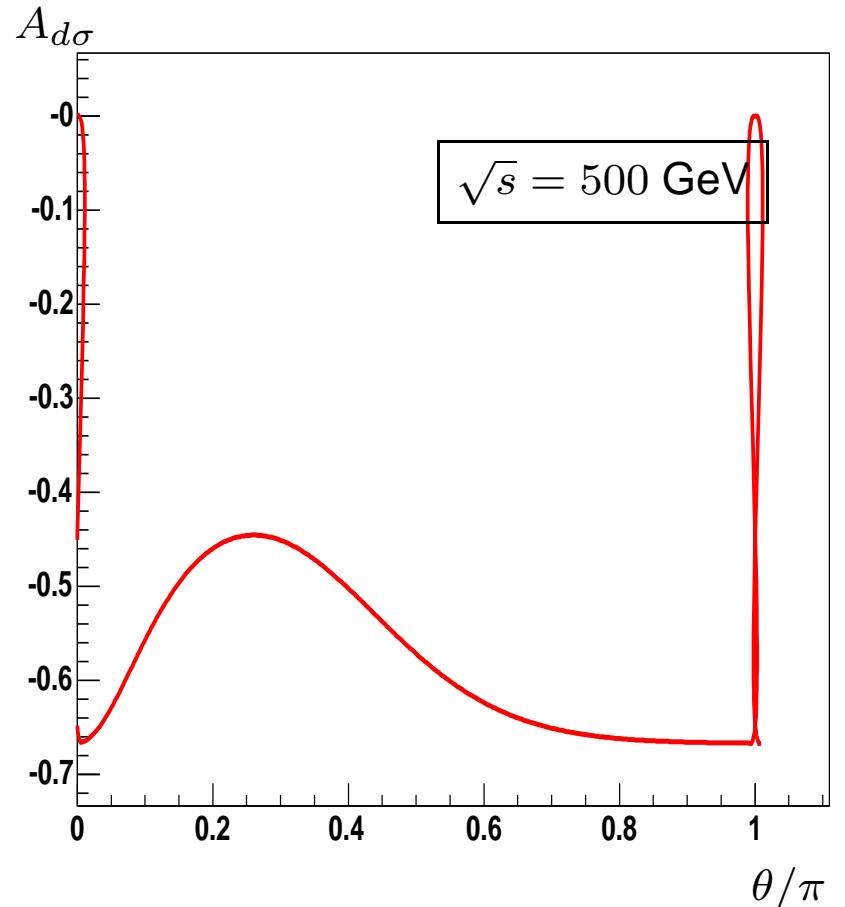
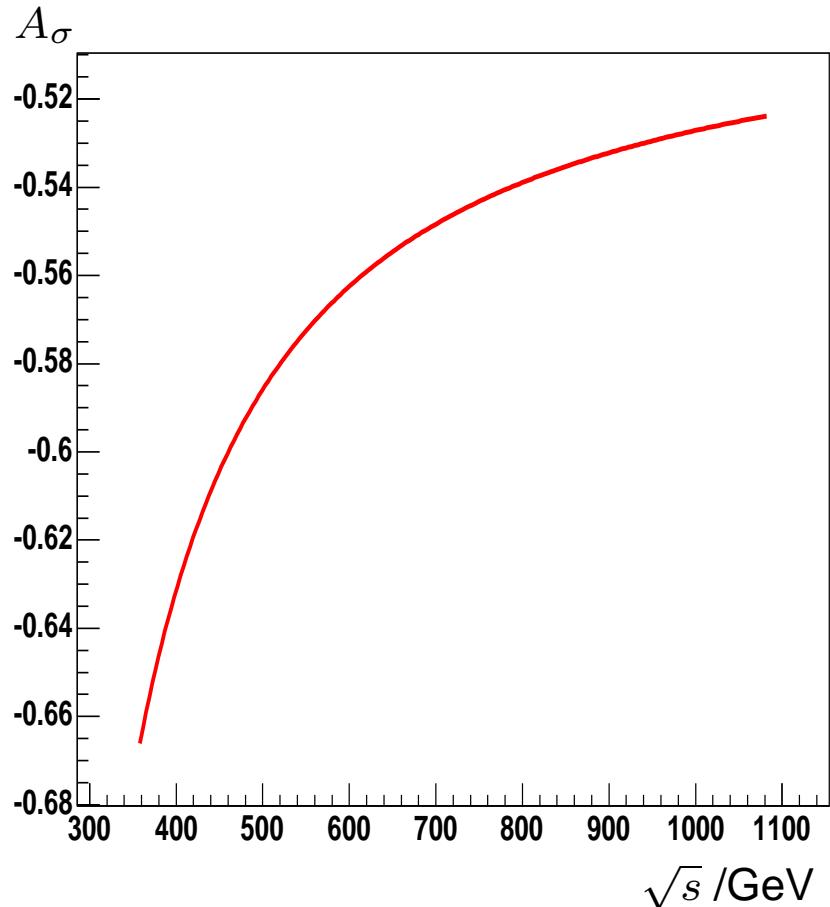


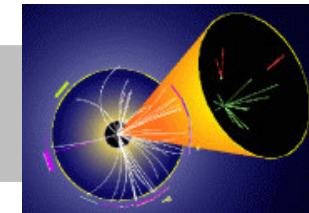
$e^- e^- \longrightarrow \tilde{\tau}_1 \tilde{e}_L$ : SPS1a-like Scenario,  $P_1^T = P_2^L = 80\%$   
 $\phi_{12} = \phi_{13} = 0.05\pi, \phi_{23} = \frac{\pi}{4}, \theta_{\tilde{\tau}} = \frac{\pi}{4}$



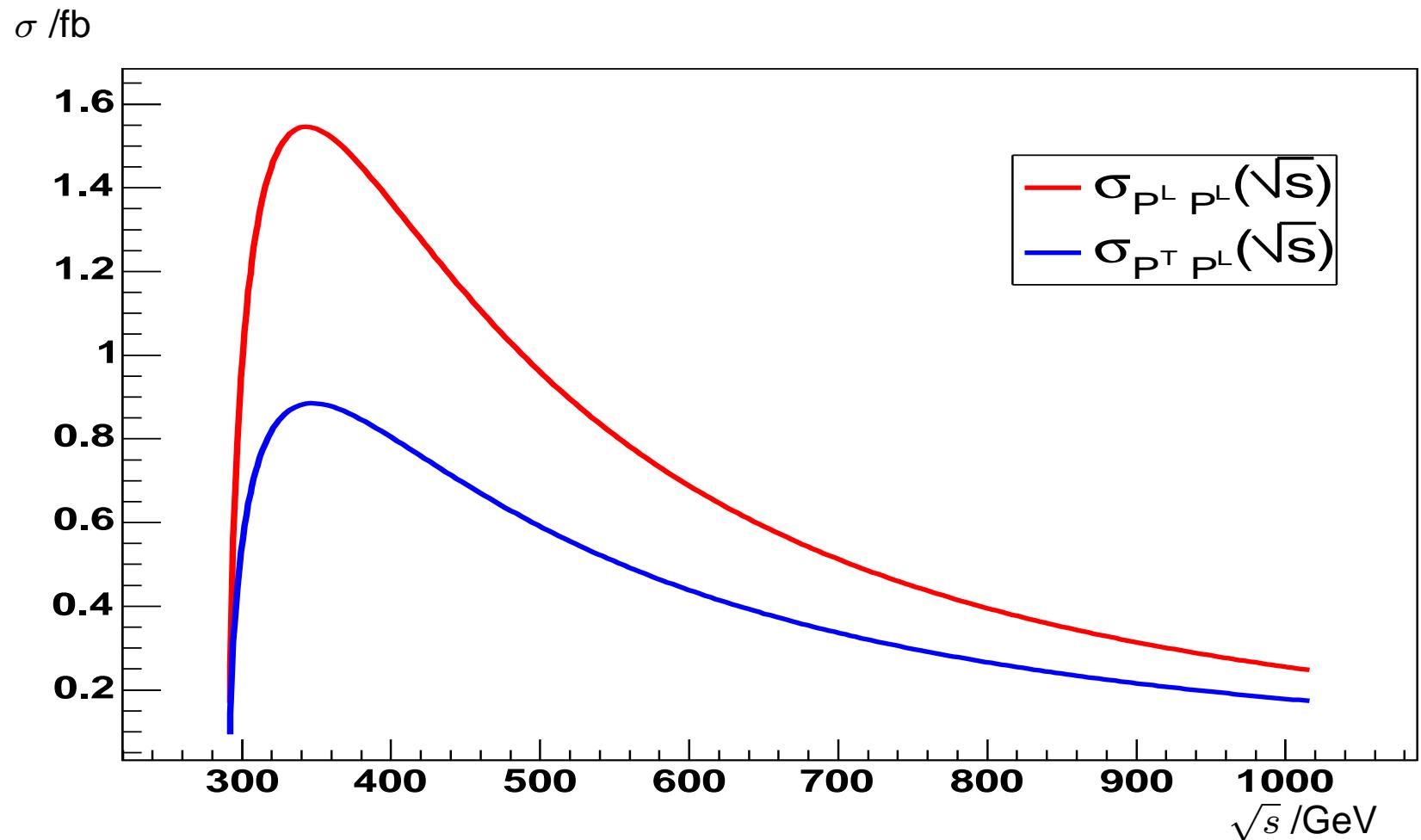
# Polarisation Asymmetries

$e^- e^- \rightarrow \tilde{\tau}_1 \tilde{e}_L$ : SPS1a-like Scenario,  $P_1^T = P_2^L = 80\%$   
 $\phi_{12} = \phi_{13} = 0.05\pi$ ,  $\phi_{23} = \frac{\pi}{4}$ ,  $\theta_{\tilde{\tau}} = \frac{\pi}{4}$

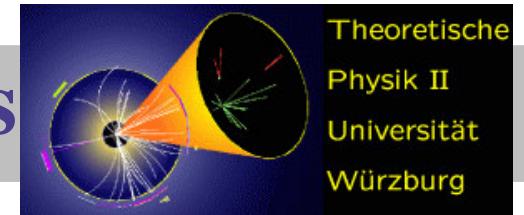




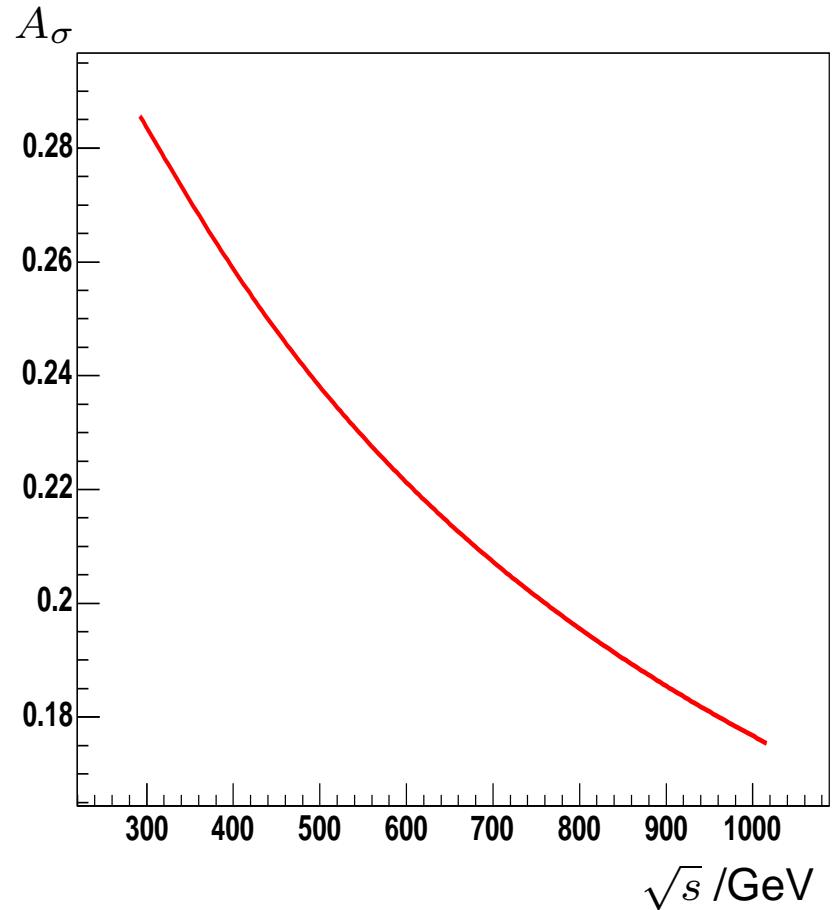
**SPS1a-like Scenario,**  $P_1^T = P_2^L = 80\%$   
 $\phi_{13} = 0.008\pi, \phi_{12} = \phi_{23} = 0, \theta_{\tilde{\tau}} = \frac{\pi}{4}$



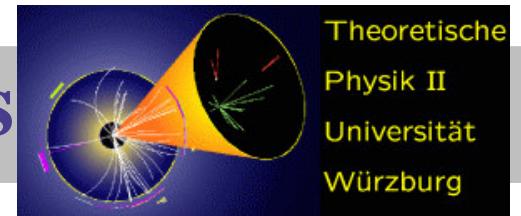
# Polarisation Asymmetries



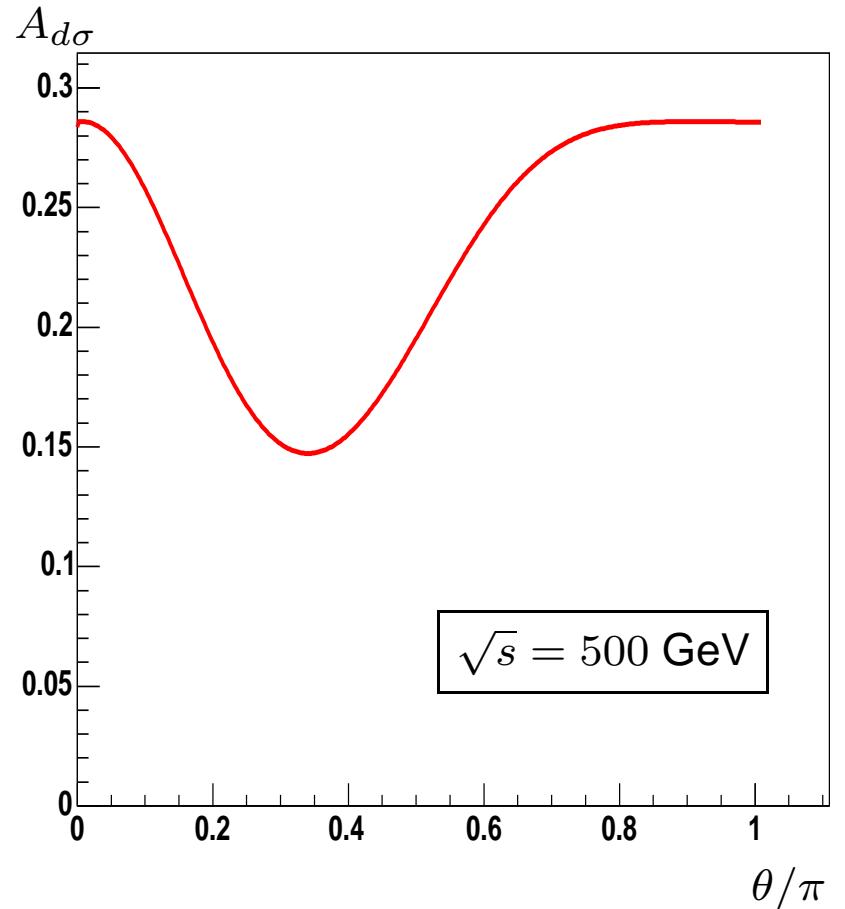
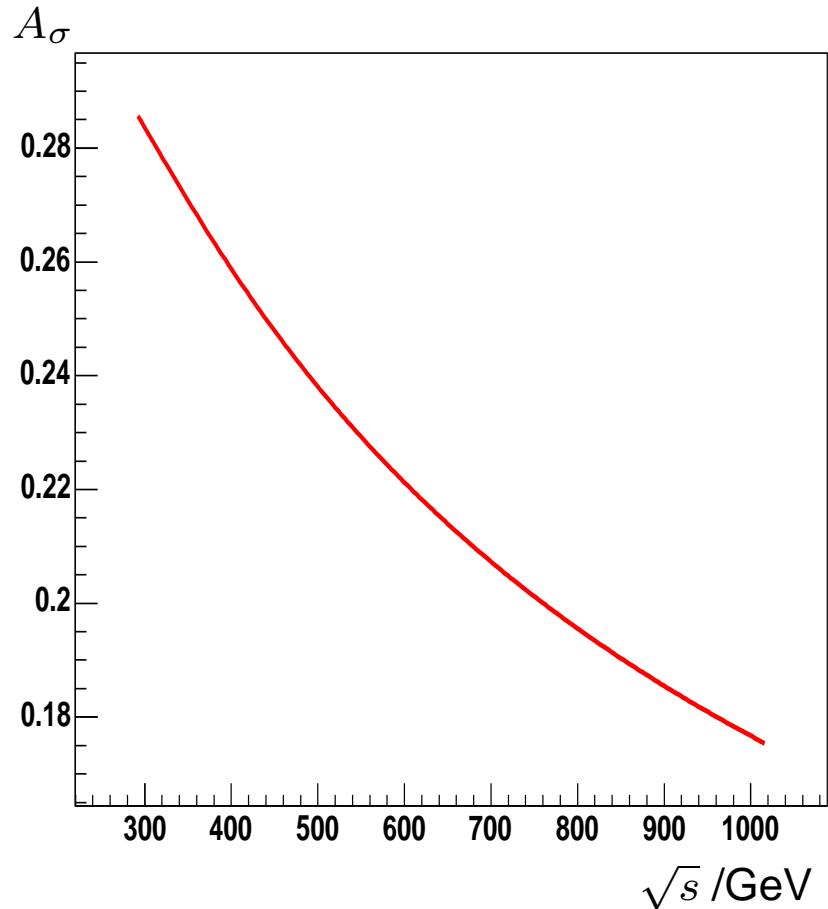
$e^- e^- \longrightarrow \tilde{\tau}_1 \tilde{e}_R$ : SPS1a-like Scenario,  $P_1^T = P_2^L = 80\%$   
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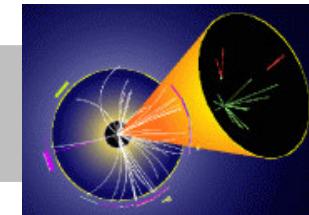


# Polarisation Asymmetries



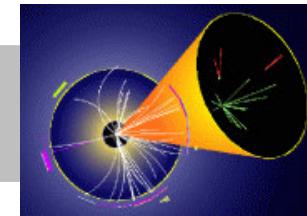
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From the couplings:

$$\begin{aligned} a_k^{m2} &= \cos \theta_{\tilde{l}} f_{\alpha k}^L W^{\alpha m}; & a_k^{m1} &= -\sin \theta_{\tilde{l}} f_{\alpha k}^L W^{\alpha(m+3)} \\ b_k^{m2} &= \sin \theta_{\tilde{l}} f_{\alpha k}^R W^{\alpha m}; & b_k^{m1} &= \cos \theta_{\tilde{l}} f_{\alpha k}^R W^{\alpha(m+3)} \end{aligned}$$



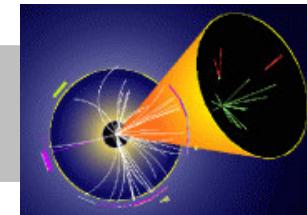
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and the structure of the linear  $P^T$ -Contributions

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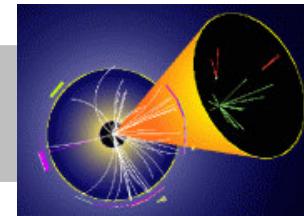
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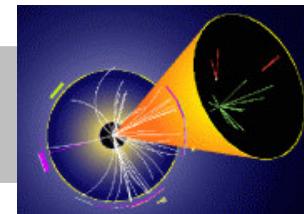
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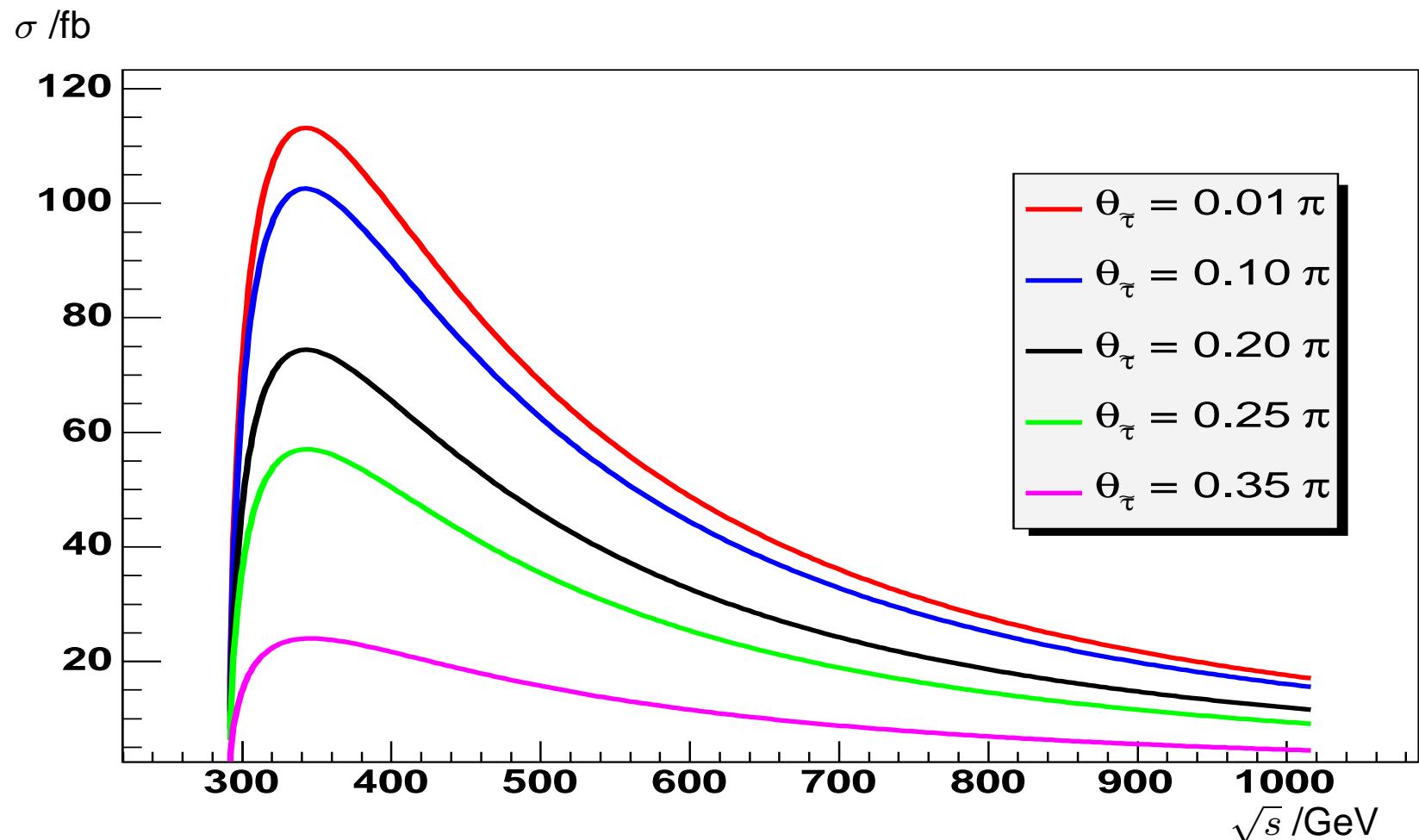
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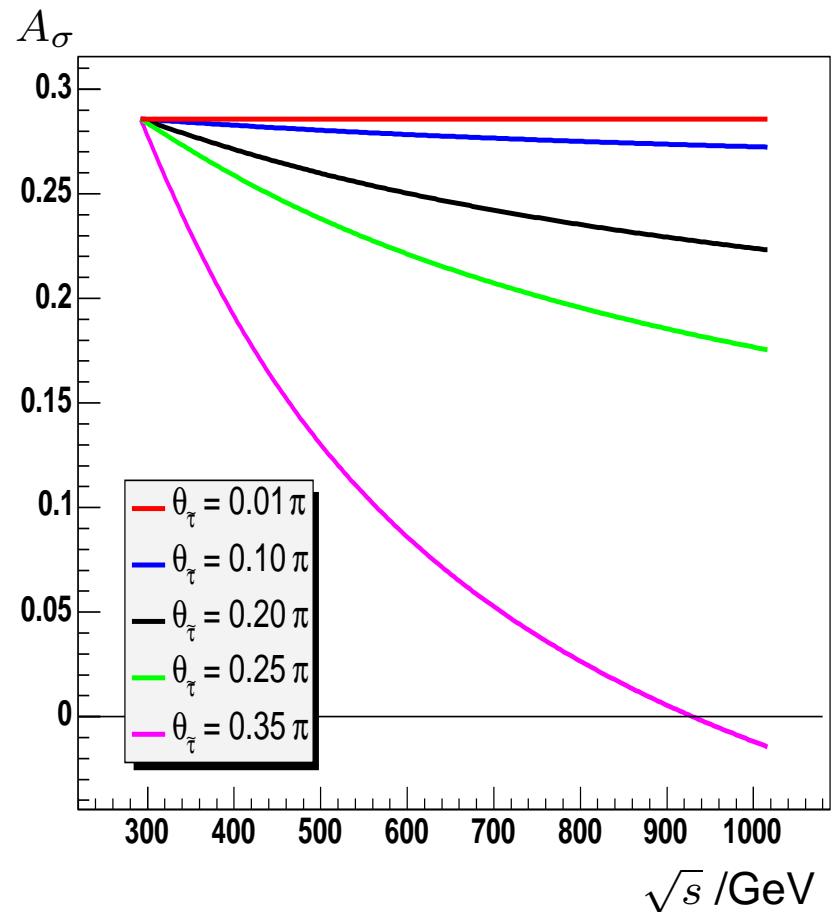
as  $\theta_{\tilde{\tau}}$  maximal, i. e.  $\approx \pi/4$   
 $\Rightarrow$  strong dependence on  $\theta_{\tilde{\tau}}$



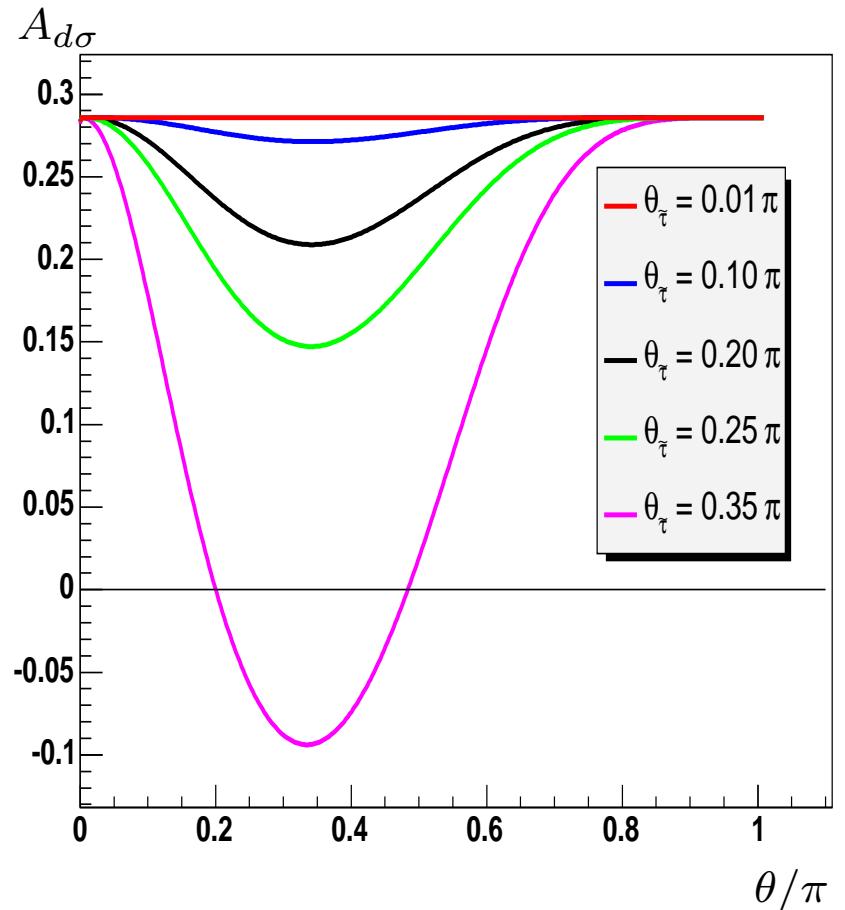
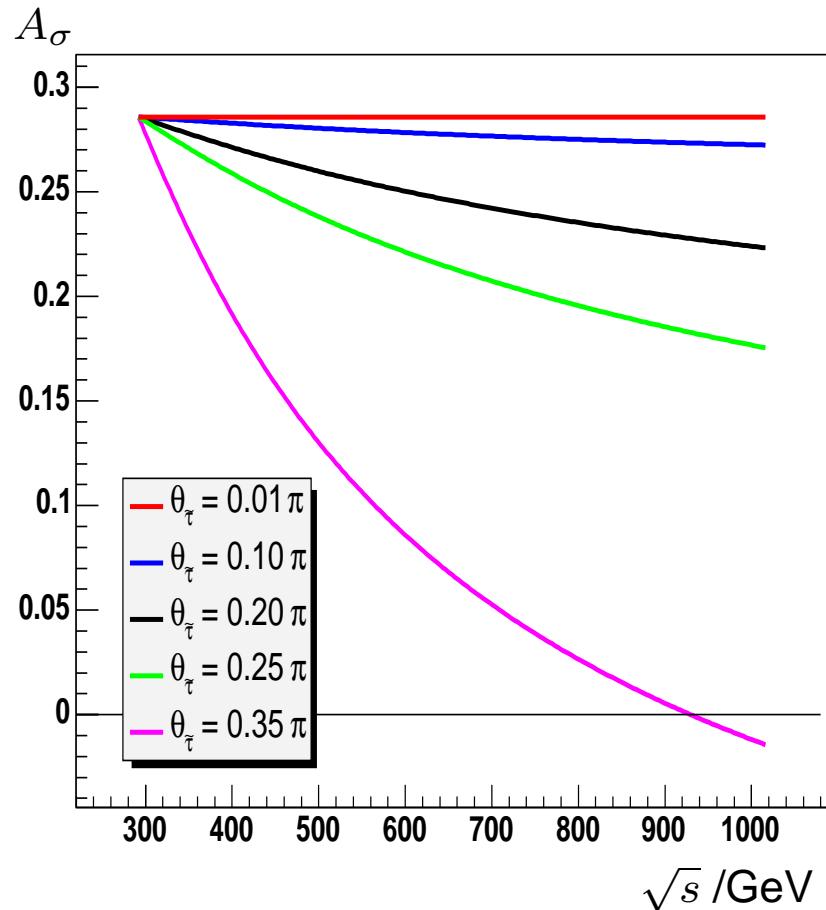
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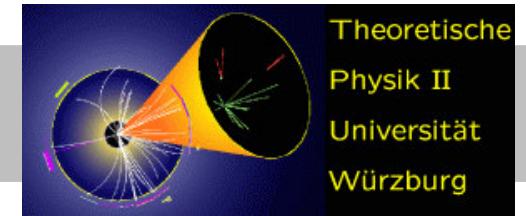


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$\langle \uparrow \diamond \downarrow \rangle$

# CP-Violation



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Here probably accessible via

- transverse polarisation
- perpendicular to the production plane

i.e. contributions of the form:

$$\langle p_2 s^a p_1 q \rangle$$

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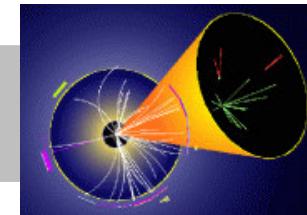
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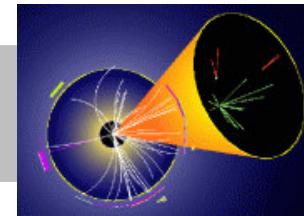
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⇒ Future investigations necessary

$\langle \uparrow \diamond \downarrow \rangle$

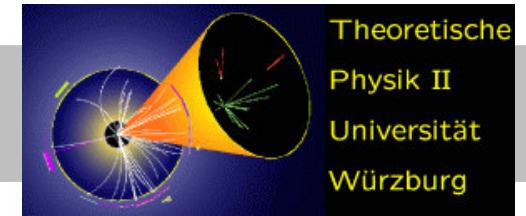
# Summary



Theoretische  
Physik II  
Universität  
Würzburg

$$e^- e^- \longrightarrow \tilde{l}_i \tilde{l}_j$$

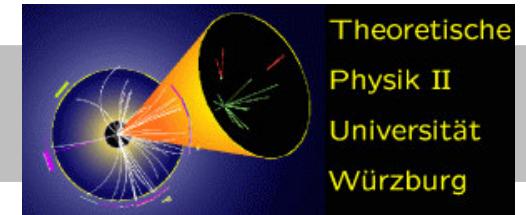
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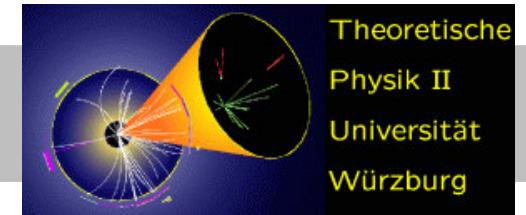
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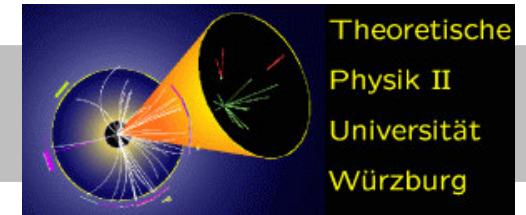
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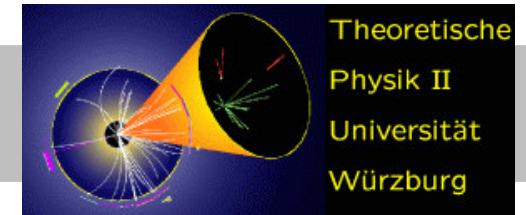
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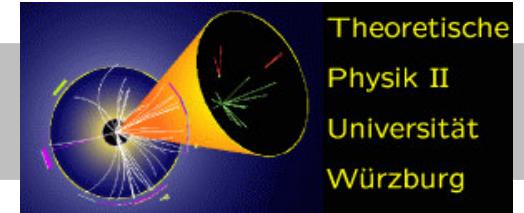
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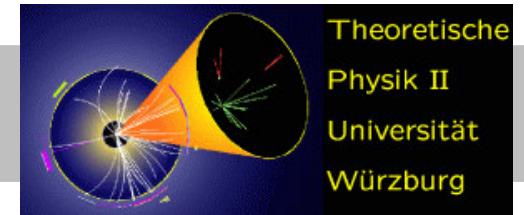
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